

$$k \leq N^2 - 2N + 2$$